

Using Crisp Sets in QCA: An Introduction

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Agenda



- **Introduce Crisp-set QCA and its mechanics** (e.g. Ragin, 1987, 2000, Ragin et al. 2006, Greckhamer et al. 2008)
- **Illustrate logic of set-theoretic analysis**

Set-theoretic Logic:

Basic Assumptions

- Causality is complex
- Cases are viewed as configurations, defined through their multiple set memberships
 - Theoretical understanding of diversity of cases
- Compare set memberships to reveal patterns of similarities/differences of cases sharing outcome
 - Identify configurations and their relationships to outcomes

Steps of Crisp Set Analysis

1. Select cases & theoretically relevant attributes
 - a) Select cases based on substantive interest
 - b) Select attributes and construct sets—Crisp sets distinguish ‘in’ (1, full membership), and ‘out’ (0, full non-membership)
2. Construct truth-tables—all logically possible configurations of included attributes
3. Analyze complex relationships between attributes and outcome of interest (necessity and sufficiency)
4. Evaluate and interpret results

I illustrate these with simple hypothetical example

Illustration: Hypothetical example of small-N setting

- RQ: What causes superior financial performance in bicycle manufacturing?
 - ▣ In this illustration I do not consider causes of absence of superior performance
- Hypothetical small-N dataset of 20 bicycle manufacturing firms, 5 attributes
 - Experience: years producing bicycles
 - R&Dintensity: R&D spending
 - NewMRP: New MRP system implemented?
 - Size: Size of the firm:
 - VertInt: Firm vertically integrated into distribution?

Step 1: Define and Establish Crisp Sets

- Define sets, including outcome:
 - “Set of large firms” (alt. “small firms”), “Set of experienced firms”, “Set of vertically integrated firms”, etc.
- Decide membership: In crisp-sets only full membership versus full non-membership (1/0)
 - Use theory and empirical knowledge to set breakpoints
- Common points of critique
 - Information loss through dichotomization
 - Potential arbitrariness of threshold
- Some responses:
 - Maintain complexity while simplifying it
 - When dichotomization is not straightforward, experiment
 - Consider fuzzy-sets to enable degrees of membership (later)

Illustration: Partial Crisp data set

Case	Experience	R&Dintense	NewMRP	FirmSize	VertIntegrated	HP
Firm1	1	0	1	1	0	0
Firm2	0	0	0	0	1	0
Firm3	1	1	1	1	1	1
Firm4	1	0	1	0	1	1
Firm5	0	0	1	0	0	0
...						

Step 2: Constructing Truth Table

- Construct Truth Table: Each row logically possible combination of crisp-sets (2^n logically possible) / Boolean expression
- Sort cases into configurations and record outcomes & consistency
 - In this example: 5 attributes = $2^n = 32$ logically possible combinations
- Code outcome value

Boolean Operators: Expressing Combinatorial Logic

- QCA uses Boolean algebra to express combinatorial logic and perform comparisons
- Logical *and* (\bullet) represents intersection of sets (\rightarrow for logical implication).
 - E.g.: $\text{size} \bullet \text{r\&intense} \rightarrow \text{superior performance}$
- Logical *or* ($+$) represents union of sets
 - E.g.: $\text{size} \bullet \text{r\&intense} + \text{age} \bullet \text{r\&intense} \rightarrow \text{superior performance}$
 - $\text{r\&intense} \bullet (\text{size} + \text{age}) \rightarrow \text{superior performance}$
- Logical *negation* (\sim)
 - $\sim \text{size}$ (0 or non-membership in set of large firms)

Simplifying Truth Table

- Boolean algebra is used to reduce truth table to expression covering combinations with same outcome (superior performance)

Simple example:

$\text{size} \cdot r \oplus \text{size} \cdot \sim r \rightarrow \text{superior performance}$

$\text{size} \cdot (r \oplus \sim r) \rightarrow \text{superior performance} =$
 $\text{size} \rightarrow \text{superior performance}$

Necessary and Sufficient conditions

- **Necessary condition:** must be present for an outcome to occur \Rightarrow when condition is necessary, all cases with outcome will exhibit causal condition
 - (e.g. all firms with superior performance are large)
- **Sufficient condition:** condition can by itself produce an outcome \Rightarrow all occurrences of condition are followed by the outcome
 - (e.g. all large firms have superior performance)

“Complex solution”

vertint•size•newmrp•experience +

(raw/unique coverage=0.625/0.5, consistency=1)

vertint•newmrp•~r&dintense•experience

(raw/unique coverage=0.37/0.25, consistency=1)

→ **Superior Performance**

(solution coverage/consistency = .875/1)

Simplified to:

vertint• experience•newmrp•(size+~r&dintense)

→ **Superior Performance**

“Parsimonious solution”

- **vertint•experience → Superior Performance**
(Raw/unique/solution coverage=.875, consistency=1)

“Intermediate solution”

□ **vertint• experience (size+~r&dintense)**

→ **Superior Performance**

(Raw/unique/solution coverage=.875, consistency=1)

Interpretation of Results

1. No component is necessary for superior performance
2. **Vertical integration into distribution, experience, implementation of new MRP system, and either experience or not R&D intensive operations associated with superior performance (core conditions bold)**
 - *Note: N too small to draw statistical inferences and conclude a combination is sufficient for high performance (Sufficiency shows only association)*

How NOT to Interpret Results

- Do not interpret “independent effects” separate from combinations
 - Firms lacking vertical integration are less likely to show superior performance (1 case with superior performance) than firms with vertical integration (7 successful cases)
 - Increased experience will incrementally increase likelihood of high financial performance of non-R&Dintensive firms
 - Size is positively associated with high financial performance in case of experienced firm

Crisp Sets: Conclusion

- Crisp sets contain basic logic of set-theoretic methods
 - Limited to 1/0 membership
 - Fuzzy set-theory is more sophisticated, relies on same principles
- Systematic comparison for small N
- Value of alternative model of causality